# WEST COVENTRY ACADEMY SIXTH FORM

West Coventry



Mathematics Department the department that counts!

## GCSE to A-LEVEL TRANSITION BOOKLET Summer 2024

## STUDENT NAME: ...

This booklet contains the important information regarding A-Level Maths to ensure that you get off to the best possible start in this subject area at A level, should you decide to enrol. This booklet also includes a range of questions from key topics that you will have seen in GCSE and will be helpful for AS Level and A-Level.

Each topic has three sections:

- Introduce questions allow you to practise the key concepts.
- Strengthen questions build on your knowledge of the key concepts.
- Deepen questions will challenge your understanding.

Use the Sparx topic codes for each topic for Independent Learning. The key facts and formulae are provided in the booklet for support. Remember to show your working out for each question.

Please hand in the completed workbook section in the first lesson if you decide to enrol to do Maths at A level. Good luck!

### **A-Level Mathematics**

#### The key staff:

Mrs Khubbar	
Mrs Rooney	

#### **Course Details**

Course Title: A level Mathematics

Exam board: Edexcel Exam Code: For AS Mathematics 8MA0 & For A Level Mathematics 9MA0 Exam Board web site: qualifications.pearson.com Assessment method: The Mathematics AS level is assessed by two final exams in year 12.

The Mathematics A level is assessed by three final exams in year 13.

#### **Minimum requirement:**

Standard entry requirements of five A\*-C grades (or equivalent 9-1 grades) including English language, along with Mathematics ideally at Grade 7 or above, but Grade 6 is considered on an individual basis.

#### About the course

This course will hopefully extend your mathematical thinking and enjoyment of the subject. The course builds strongly upon GCSE Maths, particularly the aspects of algebra, so you must be confident in these skills. You must also be prepared to think! You will have to solve problems by drawing on a number of mathematical topics and be prepared to persevere with some lengthy solutions.

#### **AS Level Mathematics**

#### Pure Mathematics – One 2-hour Exam paper.

**Topics included are:** Algebra and functions, Coordinate geometry, Trigonometry, Vectors, Exponentials and logarithms, Differentiation and Integration.

#### Mechanics and Statistics- One 1¼ hour Exam paper.

**Topics included in the statistics module are:** Statistical sampling, Data presentation and interpretation, Probability, Statistical distributions, Statistical hypothesis testing. **Topics included in the mechanics module are:** Quantities and units in mechanics, Kinematics and Forces and Newton's laws.

#### **A Level Mathematics**

#### Pure Maths – Two 2-hour Exam papers.

**Topics included are:** Algebra and functions, Coordinate geometry, Trigonometry, 2D Vectors, Exponentials and logarithms, Differentiation and Integration. Proof, Algebraic & partial fractions, Functions and modelling, Series & sequences, Binomial theorem, Trigonometry, Parametric equations, Differentiation, Numerical methods, Integration and 3D Vectors.

#### Mechanics and Statistics - One 2-hour Exam paper.

**Topics included in the statistics module are:** Statistical sampling, Data presentation and interpretation, Probability, Statistical distributions, Statistical hypothesis testing, Regression and correlation, Normal distribution

**Topics included in the mechanics module are:** Quantities and units in mechanics, Kinematics, Forces & Newton's laws, Moments and Forces at any angle.

#### Academic and Career Pathways

Apart from further study of Mathematics itself, many university courses depend on the subject. For example, Science, Computing and Engineering based courses use a great deal of mathematics. Subjects such as Geography, Psychology, Economics and Business make use of Statistics. Mathematics is also a requirement for Finance and Accountancy training. It is reported that people with A Level Mathematics are earning an average of 10% more than others.

#### What equipment will be needed for the subject?

An A4 ring binder, with dividers Lined paper Pens, pencils, ruler A scientific calculator, capable of dealing with data analysis of a large data set. We recommend the Casio Classwiz fx-991EX.

PLEASE CONSULT WITH THE MATHS DEPARTMENT BEFORE BUYING ANY OTHER MODEL.

#### **Text Books**

Students will have access to the digital textbooks for both AS and AL. For those students who wish to have paperback textbooks also, then students are required to pay a refundable deposit of £10 for each of the two textbooks needed for AS Maths and £10 deposit for each of the two AL books. The deposits will be returned to the students on return of the textbooks in a reusable condition.

In this booklet, there are a range of questions from key topics that you will have seen in GCSE and will be helpful for AS Level and A-Level.

Each topic has three sections:

- **Introduce** questions allow you to practise the key concepts.
- **Strengthen** questions build on your knowledge of the key concepts.
- **Deepen** questions will challenge your understanding.

Unless otherwise indicated, you may use a calculator.

Use the grid below to keep track of your progress in each topic. Tick the sections you have attempted. If you use Sparx Maths you can find even more questions by searching for the Sparx topic codes in Independent Learning.

	I.	S	D	Sparx topic codes	Teacher comment
Surds	0	0	0	U499 U707 U281	
Expanding brackets	0	0	$\bigcirc$	U768 U606	
Factorising quadratics	0	0	$\bigcirc$	U178 U858	
Simplifying expressions	0	0	0	U662 U437	
Operations with algebraic fractions	0	0	0	U685 U457 U824	
Solving quadratic equations	0	$\bigcirc$	0	U228 U960 U665 U150	
Quadratic graphs	$\bigcirc$	$\bigcirc$	0	U589 U769 U601	
Linear simultaneous equations	0	0	$\bigcirc$	U760 U757	
Straight-line graphs	0	0	$\bigcirc$	U315 U477 U848 U669 U377 U898	
Right-angled trigonometry	0	0	$\bigcirc$	U283 U545 U170	
Further trigonometry	0	0	$\bigcirc$	U952 U591	

## Key facts and formulae:

#### The Quadratic formula:

The solution of 
$$ax^2 + bx + c = 0$$

where  $a \neq 0$ 

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

#### Trigonometry:

In any right-angled triangle ABC where a, b and c are the length of the sides and c is the hypotenuse:

$$\sin A = \frac{a}{c}$$
  $\cos A = \frac{b}{c}$   $\tan A = \frac{a}{b}$ 



In any triangle ABC where a, b and c are the length of the sides:

sine rule: 
$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

cosine rule:  $a^2 = b^2 + c^2 - 2bc \cos A$ 





Q4	Write $(5 + \sqrt{12})(11 + \sqrt{3})$ in the form $a + b\sqrt{3}$ , where $a$ and $b$ are integers.
	Answer:
	1 . /2
Q5	Rationalise the denominator of $\frac{1+\sqrt{2}}{\sqrt{2}}$
	Give your answer as a fraction in its simplest form.
	Answer:

Expand and fully simplify $(2\sqrt{6} - 5\sqrt{2})^2$
Expand and fully simplify $(2\sqrt{6} - 5\sqrt{2})^2$ Answer: Rationalise the denominator of $\frac{15 + \sqrt{3}}{10\sqrt{3}}$ Give your answer as a fraction in its simplest form.
Answer:

Strengthen



Q3	Rationalise the denominator of $\frac{2\sqrt{7}}{3+\sqrt{7}}$
	Give your answer in its simplest form.
	A recovery
	Answer:
Q4	Write $\sqrt{12} + \frac{33}{12}$ in the form $r/3$ , where r is an integer.
	$\sqrt{3}$
	Answer:







Q1	Expand and fully simplify ( $m$ + 9)( $m$ + 2)
	Answer:
Q2	Expand and fully simplify (2 $a$ + 3)(4 $a$ + 5)
	Answer:

Introduce

Q3	Expand and fully simplify ( $x$ - 3)(4 $x$ + 9)
	Answer:
Q4	Expand and fully simplify $(6n - 5)^2$
	Answer:

Introduce

Q1	Expand and fully simplify $2(4d + 5)(3d + 1)$
	Answer:
Q2	Expand and fully simplify $(x + 1)(x^2 + 3x + 5)$
	Answer:

Strengthen

Q3	Expand and fully simplify $(3n + 4)(5n + 2) + 5(n + 7)$
	Answer:
-	
Q4	Expand and fully simplify $(t - 2)(t + 5)(t - 4)$
	Answer:



Q4

Write the following expression in the form  $\frac{1}{ax^b} + \frac{1}{cy^d}$  where a, b, c, and d are integers.

$$\left(\frac{1}{5x} + \frac{1}{4y}\right) \left(\frac{1}{25x^2} - \frac{1}{20xy} + \frac{1}{16y^2}\right)$$

Answer:

Show that  $(x^{2} + 1)(y^{2} + 4) \equiv (xy - 2)^{2} + (2x + y)^{2}$ 





Strengthen

Q1	Fully factorise $x^2$ - 16	
		Answer:
Q2	Fully factorise $2r^2$ + 15 $r$ + 7	
		Answer:
Q3	Fully factorise $5x^2 + 22x + 8$	
		Answer:





Fully simplify the expression 4  $y^{5}$  x 3  $y^{2}$ **Q1** Answer: Simplify  $(h^{-5})^3$ Q2 Give your answer without any negative indices. Answer: Write  $\frac{2t^6u}{8t^3}$  as a fraction in its simplest form. Q3 Answer:

#### Simplifying expressions

Introduce

Fully simplify  $\left(\frac{t^3}{u^5}\right)^2$ Q4 Answer: Write  $\frac{33xy + 9x}{18x}$  as a fraction in its simplest form. **Q5** Answer: Fully simplify  $\frac{6a + 42}{a^2 + 11a + 28}$ Q6 Answer:

#### Simplifying expressions

Strengthen







Introduce

**Q1** Fully simplify  $\frac{14a}{b} \times \frac{b}{2}$ Answer: Q2 Fully simplify  $\frac{6a}{v} \div \frac{2a}{5}$ Give your answer as a fraction. Answer: Fully simplify the expression below to give a single fraction. Q3  $\frac{n+2}{5} + \frac{6n}{7}$ Answer:



**Q1** Fully simplify 
$$\frac{2}{5a+4} \times \frac{45a+36}{a}$$
  
Give your answer as a fraction.  
Answer: \_\_\_\_\_\_  
**Q2** Fully simplify  $\frac{6x}{(5x-7)(x+1)} = \frac{1}{5x-7}$   
Give your answer fully factorised.

Q3	Write the following as a single fraction in its simplest form: $\frac{2x^2 - 11x + 12}{2x^2 - 6x}$
	x + 5 Give your answer fully factorised.
	Answer:
Q4	Fully simplify $\frac{4ab^2}{k} \times \frac{3ak}{12k} \times \frac{7}{5ab}$
	Give your answer as a fraction.
	Answer:

Strengthen



Q2

Fully simplify 
$$\frac{7}{36-x^2} - \frac{3}{6+x}$$

Give your answer fully factorised.

Answer:

\_\_\_\_\_

Write the following as a single fraction in its simplest form:

$$6 - (x + 4) \div \frac{x^2 + 11x + 28}{x - 7}$$

Give your answer fully factorised.

Answer:







Introduce







Q3	Using the quadratic formula, solve $6x^2 - 35 = -11x$
	Answer:
Q4	Solve $3r(3r - 4) = 2$
	Give your answers to 2 d.p.
	Answer:



Q1	Solve $x(x+4) - 4(5x+9) = 0$
	Answer:
Q2	Jessica thinks of a positive number, $n$ , which is less than 1 She adds this number to its reciprocal and gets 2.9
	Work out the value of $n$ . Give your answer as a fraction in its simplest form.
	Answer:



Solve 
$$\frac{4}{y-1} - \frac{5}{y+2} = \frac{3}{y}$$
  
Answer: \_\_\_\_\_\_  
Q4  $x = \frac{-3 \pm \sqrt{29}}{2}$   
There is only one equation of the form  $x^2 + bx + c = 0$  that gives these values of  $x$  as solutions.  
Work out the values of  $b$  and  $c$ .



Q1

Introduce

Q4

The diagram below shows the graph of the function  $y = 2x^2 + 2x - 7$ Work out the solutions to  $2x^2 + 2x - 7 = -3$ у 2-1 0 -4 -3 -2 -1 ż -1 -2 -3 -4 -5 -6-Answer: Write  $x^2 + 6x + 11$  in the form  $(x + c)^2 + d$ , where c and d are numbers. a) Answer: a) Hence, write down the coordinates of the turning point on the curve b)  $y = x^{2} + 6x + 11$ Answer: b) ( \_\_\_\_\_)

**Sparx Maths** 

Introduce



The diagram below shows a sketch of the curve y =  $x^2$  + 8x - 10

P is the turning point of the curve.

Work out the coordinates of P.

y y y y y P Answer: (\_\_\_\_\_\_)

Work out the coordinates of the turning point of the curve  $y = x^2 - 5x + 1$ 

Answer: ( \_\_\_\_\_, \_\_\_\_)

Q1





P is the turning point of the curve.

Work out the coordinates of P.



The diagram below shows the graph of  $y = 2x^2 - 5x - 3$ 

Use the diagram to estimate the solutions to  $2x^2 - 5x - 3 = -2x + 2$ Give any decimal answers to 1 d.p.



Answer:

Q3





The diagram below shows the graph of  $y = 2x^2 + 4x - 1$ The equation  $2x^2 + 4x - 1 = k$  has solutions at x = -3 and x = 1

What is the value of k?





- A curve has the equation  $y = -x^2 + 16x 65$
- a) Work out the turning point of the curve.

Answer: a) ( \_\_\_\_\_\_)

b) By considering the position of the turning point and the shape of the curve, work out how many real roots  $y = -x^2 + 16x - 65$  has.

Answer: b)















Q4

Solve the following simultaneous equations:

$$7y + 2x = \frac{23}{2}$$
  
 $5y + 3x = 9$   
Answer:  $x = \dots y = \dots$   
Solve the following simultaneous equations:  
 $4.6t + 8.1u = 104$   
 $3.8t - 2.7u = -8$ 







Q4

Solve the following simultaneous equations:

$$\frac{4}{7x-4} = \frac{1}{6y}$$

$$\frac{5x}{3y+2} = 4$$
Answer:  $x = \dots$   $y = \dots$ 
Solve the following simultaneous equations:
$$2^{x} = 4^{(7-2y)}$$

$$3^{(5x-13y)} = 81$$

*x* = \_\_\_\_\_

Answer:

*y* = \_\_\_\_\_



Introduce

	Straight-line graphs Introduce
Q4	A straight line has a gradient of 3 and passes through the point (2, 10) Work out the equation of the line.
	Answer:
Q5	Work out the equation of the straight line that passes through (2, 3) and (5, 18)
	Answer:

Strengthen

Q1	A straight line has a gradient of $-\frac{3}{4}$ , and passes through the point (32, 12)
	Work out the equation of the line.
	Answer:
Q2	The diagram below shows point P and Line A. Line B is <b>perpendicular</b> to line A and passes through point P.
	What is the equation of line B?
	y $x^{P(3,5)}$ x y x x x
	$\sqrt{y}=-3x+8$
	Answer:

Work out the equation of the straight line that passes through (1, -7) and (6, 8) Q3 Answer: The graph below shows line P and line Q. Q4 Line Q is **parallel** to line P. What is the equation of line Q? Line Q  $\boldsymbol{y}$ Line P (9, 14) (2, 11)(5, 2)  $\mathbf{x}$ Answer: 

Strengthen



Write an expression, in terms of h, for the gradient of a line **perpendicular** to the **Q1** line segment joining (3h, 20) to (6h, 8)Give your answer as a fully simplified fraction. Answer: The triangle ABC has an area of 24 square units. Q2 What are the coordinates of point B? y 20 В x 15 Answer: ( \_\_\_\_\_ )

Q4





Work out the ratio of the length of OQ to the length of OR. Give your answer in its simplest form.



A circle, centre O, passes through the point (6, -12), as shown.

Work out the equation of the tangent to the circle at this point. Give your answer in the form y = mx + c, where m and c are integers or fractions in their simplest form.



















The graph below shows the line with equation y = 5x + 2The axes both have the same scale.

Calculate the size of angle  $\theta$ . Give your answer in degrees to the nearest integer.



**Q3** 

Q4

![](_page_56_Picture_1.jpeg)

Q2

Using the sine rule, calculate the length x. Give your answer to 1 d.p. 40  $\boldsymbol{x}$ 57° 9 cm Not drawn accurately Answer: \_\_\_\_\_ cm Using the cosine rule, work out the length y. Give your answer to 1 d.p. 65° 6 m 11 m y Not drawn accurately Answer: \_\_\_\_\_ m

![](_page_57_Picture_1.jpeg)

![](_page_57_Figure_3.jpeg)

![](_page_58_Picture_1.jpeg)

![](_page_58_Figure_2.jpeg)

![](_page_59_Picture_1.jpeg)

![](_page_59_Picture_2.jpeg)

![](_page_60_Picture_1.jpeg)

![](_page_60_Figure_2.jpeg)